



Topology Seminar at Texas State

Friday, 2019, April 19, 11:00-11:50 a.m., in DERR 333

Speaker: Dr. Weam Al-Tameemi

Topic: *Semi-direct Products in Polish Groups*

ABSTRACT

The research interests of topological groups range over all aspects of modern-day topology and algebra. For example, the methods introduced in this presentation is a combination of descriptive set theory on Polish groups and some results from group actions. For example, is there a semidirect product $\mathbb{R}^n \times G(n)$, where $G(n)$ is one of the following Polish groups?

1. $GL(n, \mathbb{R}) = \{A \in M(n, \mathbb{R}) : \det(A) \neq 0\}$, or
2. $SL(n, \mathbb{R}) = \{A \in GL(n, \mathbb{R}) : \det(A) = 1\}$, or
3. $|SL(n, \mathbb{R})| = \{A \in GL(n, \mathbb{R}) : |\det(A)| = 1\}$, or
4. $GL_+(n, \mathbb{R}) = \{A \in GL(n, \mathbb{R}) : \det(A) > 0\}$.

We say that a Polish group G is an algebraically determined if given any Polish group L and an algebraic isomorphism $\varphi : L \rightarrow G$, then φ is a topological isomorphism.

In this direction the results of the work on the semidirect product $\mathbb{R}^n \times G(n)$ can also be generalized to different semidirect products constructed from groups of special interest. The key to such problems is to determine which sets in a Polish group are definable both algebraically and topologically.