



Topology Seminar at Texas State

**When:** Friday, April 28, 2023, 11:00 a.m.

**Where:** DERR 333 *and* ZOOM (Zoom info at bottom of page)

**Presenter:** Dr. Sean Corrigan

**Title:** Milnor's Exotic 7-sphere

**Abstract:** We will revisit John Milnor's famous 1956 construction of some smooth manifolds which are homeomorphic, but not diffeomorphic, to the standard 7-sphere. The constructions are those of fiber bundles whose base spaces are the 4-sphere and whose fibers are the 3-sphere. Their classification up to homeomorphism utilizes a classic result of Morse theory, while the diffeomorphism classification involves a numeric invariant defined by Milnor. The definition of this numeric invariant makes clever use of some major topological breakthroughs that occurred in the mid-1950s, and the resulting examples remain a testament to the profound way in which algebra breathes life into topology.

**The number of different differentiable structures on spheres in low dimensions**

|              |   |   |   |   |   |   |    |   |   |    |     |    |    |    |       |    |    |    |
|--------------|---|---|---|---|---|---|----|---|---|----|-----|----|----|----|-------|----|----|----|
| dimension    | 1 | 2 | 3 | 4 | 5 | 6 | 7  | 8 | 9 | 10 | 11  | 12 | 13 | 14 | 15    | 16 | 17 | 18 |
| # structures | 1 | 1 | 1 | ? | 1 | 1 | 28 | 2 | 8 | 6  | 992 | 1  | 3  | 2  | 16256 | 2  | 16 | 16 |

**Zoom Information**

**Meeting URL (click this)**

**Meeting ID: 977 0390 3382**

**Password: manifolds**